

AMENDMENTS TO THE CLAIMS

1. **(Currently Amended)** A public key generation apparatus including:
 - a random number generator for generating a random number ka that holds a relationship $0 < ka < q$, where an element in a finite group F for which multiplication is defined is g , and an order that is a prime number of the element g is q ; and
 - a public key generator for calculating a public key ya in the finite group F from the random number ka , the element g , and the prime number q ,

wherein at least said random number generator and said public key generator are being formed on one semiconductor integrated circuit, and

wherein a controller of a first user as a distribution source of the public key controls controlling the random number generator and the public key generator for obtaining to obtain the public key ya , and transmits transmitting the obtained public key ya to a second user as a distribution destination of the public key.
2. **(Currently Amended)** The public key generation apparatus of Claim 1, wherein said public key generator calculates the public key ya in the finite group F by a formula:
$$ya = g^ka \bmod q$$
, using the random number ka , the element g , and the prime number q .
3. **(Currently Amended)** The public key generation apparatus of Claim 1, wherein when the finite group F is an elliptic curve $E(F)$ in a finite field, and an element of the elliptic curve $E(F)$ is G ,
said public key generator calculates the public key ya on the elliptic curve $E(F)$ by a

formula: $ya = kaG \bmod q$, using the random number ka , the element G , and the prime number q .

4. **(Currently Amended)** The public key generation apparatus of Claim 1, wherein said random number generator generates a new random number ka after the calculation of the public key ya is completed.

5. **(Currently Amended)** A shared key generation apparatus including:
a random number generator for generating a random number ka that holds a relationship $0 < ka < q$, where an element in a finite group F for which multiplication is defined is g , and an order that is a prime number of the element g is q ; and
a shared key generator for calculating a shared key Ka in the finite group F from a public key yb that is generated from a random number kb which holds a relationship $0 < kb < q$ and is generated by a second user as a distribution destination of the shared key, and the random number ka ,

wherein at least said random number generator and said shared key generator are being formed on one semiconductor integrated circuit, and

wherein a controller of a first user as a distribution source of the shared key obtaining obtains the public key yb from the second user as the shared key distribution destination, and controlling controls the random number generator and the shared key generator for deriving to derive the shared key Ka .

6. **(Currently Amended)** The shared key generation apparatus of Claim 5, wherein said shared key generator ~~calculates~~ calculates the shared key K_a in the finite group F by a formula: $K_a = y_b^{k_a} \bmod q$, using the public key $y_b = g^{k_b} \bmod q$ which is generated by the second user as the shared key distribution destination and the random number k_a .

7. **(Currently Amended)** The shared key generation apparatus of Claim 5, wherein when the finite group F is an elliptic curve $E(F)$ in a finite field and an element of the elliptic curve $E(F)$ is G ,

said shared key generator calculates the shared key K_a on the elliptic curve $E(F)$ by a formula: $K_a = k_a y_b \bmod q$, using the public key $y_b = k_b G \bmod q$ which is generated on the elliptic curve $E(F)$ from the random number k_b by the second user as the shared key distribution destination, and the random number $[[k]] k_a$.

8. **(Currently Amended)** The shared key generation apparatus of Claim 5, wherein said random number generator generates a new random number k_a after the calculation of the shared key K_a is completed.

9. **(Currently Amended)** A key exchange apparatus including:
a random number generator for generating a random number k_a that holds a relationship $0 < k_a < q$, where an element in a finite group F for which multiplication is defined is g , and an order that is a prime number of the element g is q ;
a public key generator for calculating a public key y_a in the finite group F from the

random number ka , the element g , and the prime number q ; and

a shared key generator for calculating a shared key Ka in the finite group F on the basis of the public key yb generated from a random number kb which holds a relationship $0 < kb < q$ and is generated by a second user as a distribution destination of the shared key, and the random number ka ,

wherein at least said random number generator, said public key generator, and said shared key generator ~~being~~are formed on one semiconductor integrated circuit, and wherein a controller of a first user as a distribution source of the shared key ~~controlling~~controls the random number generator and the public key generator ~~for obtaining~~to obtain the public key yb , and ~~controlling~~controls the shared key generation unit ~~for deriving~~to derive the shared key $[[ka]] Ka$.

10. **(Currently Amended)** The key exchange apparatus of Claim 9, wherein

 said public key generator calculates the public key ya in the finite group F by a formula:
 $ya = g^ka \bmod q$, using the random number ka , the element g , and the prime number q , and
 said shared key generator calculates the shared key Ka in the finite group F by a formula:
 $Ka = yb^ka \bmod q$, using the public key $yb = g^kb \bmod q$ which is generated in the finite group F by the second user as the shared key distribution destination using the random number kb , and the random number ka .

11. **(Currently Amended)** The key exchange apparatus of Claim 9, wherein

 when the finite group F is an elliptic curve $E(F)$ in a finite field, and an element of the

elliptic curve $E(F)$ is G ,

 said public key generator calculates the public key ya on the elliptic curve $E(F)$ by a formula: $ya = kaG \bmod q$, using the random number ka , the element G , and the prime number q , and

 said shared key generator calculates the shared key Ka on the elliptic curve $E(F)$ by a formula: $Ka = kayb \bmod q$, using the public key $yb = kbG \bmod q$ generated from the random number kb on the elliptic curve $E(F)$ by the second user as the shared key distribution destination, and the random number ka .

12. **(Currently Amended)** The key exchange apparatus of Claim 9, wherein the random number generator generates a new random number ka after the calculation of the public key ya and the calculation of the shared key Ka are both completed.

13. **(Currently Amended)** A key exchange apparatus including:

- a random number generator for generating a random number ka that holds a relationship $0 < ka < q$, where an element in a finite group F for which multiplication is defined is g , and an order that is a prime number of the element g is q ;
- a secret key holding unit for temporarily holding the random number ka ;
- a public key generator for calculating a public key ya in the finite group F from the random number ka , the element g , and the prime number q ; and
- a shared key generator for calculating a shared key Ka in the finite group F using a public key yb generated from a random number kb which holds a relationship $0 < kb < q$ and is

generated by a second user as a destination distribution of the shared key, and the random number ka that is held by the secret key holding unit,

wherein at least said random number generator, said secret key holding unit, said public key generator, and the shared key generator ~~being~~are formed on one semiconductor integrated circuit,

wherein a controller of a first user as a distribution source of the shared key ~~controlling~~controls the random number generator and the public key generator ~~for obtaining~~to obtain the public key ya, and ~~transmitting~~transmits the obtained public key ya to a second user as a distribution destination of the shared key, and

wherein said controller ~~obtaining~~obtains the public key yb from the second user as the shared key distribution destination, and ~~controlling~~controls the shared key generator ~~for deriving~~to derive the shared key Ka.

14. **(Currently Amended)** The key exchange apparatus of Claim 13, wherein the public key generator calculates the public key ya in the finite group F using the random number ka, the element g, and the prime number q by a formula: $ya = g^ka \bmod q$, and the shared key generator calculates the shared key Ka in the finite group F by a formula: $Ka = yb^ka \bmod q$, using the public key yb = $g^{kb} \bmod q$ that is generated in the finite group F from the random number kb by the second user as the shared key distribution destination, and the random number ka that is held in the secret key holding unit.

15. **(Currently Amended)** The key exchange apparatus of Claim 13, wherein

when the finite group F is an elliptic curve E(F) in a finite field, and an element on the elliptic curve E(F) is G,

the public key generator calculates the public key ya on the elliptic curve E(F) using the random number ka, the element G, and the prime number q by a formula: $ya = kaG \bmod q$, and

the shared key generator calculates the shared key Ka on the elliptic curve E(F) by a formula: $Ka = Kayb \bmod q$, using the public key $yb = kbG \bmod q$ that is generated from the random number kb on the elliptic curve E(F) by the second user as the shared key distribution destination, and the random number ka that is held in the secret key holding unit.

16. **(Currently Amended)** The key exchange apparatus of Claim 13, wherein
the random number generator generates a new random number ka after the calculation
of the public key ya is completed, and
the secret key holding unit holds the new random number ka generated by the random
number generator.

17. **(Currently Amended)** The key exchange apparatus of Claim 13, wherein
the random number generator generates a new random number ka after the calculation
of the shared key Ka is completed, and
the secret key holding unit holds the new random number ka generated by the random
number generator.

18. **(Previously Presented)** A key exchanging method that employs the key exchange

apparatus of Claim 9, thereby exchanging the public keys that are generated by a first user and a second user that intend to exchange the public keys, respectively, to generate a shared key by the first user and the second user on the basis of the exchanged public key, respectively.

19. **(Previously Presented)** A key exchanging method that employs the key exchange apparatus of Claim 13, thereby exchanging the public keys that are generated by a first user and a second user that intend to exchange the public keys, respectively, to generate a shared key by the first user and the second user on the basis of the exchanged public key, respectively.